

Finding the Boltzmann Constant through the Evaporation of Ethanol and the Formaldehyde Clock Reaction.

Mustafa Afzal.

The Formaldehyde Clock Reaction – Theory.

- Solution A →

5 g of Anhydrous Sodium diSulfite +
1 g of Anhydrous Sodium Sulfite +
1 L of Distilled Water.

- Solution B →

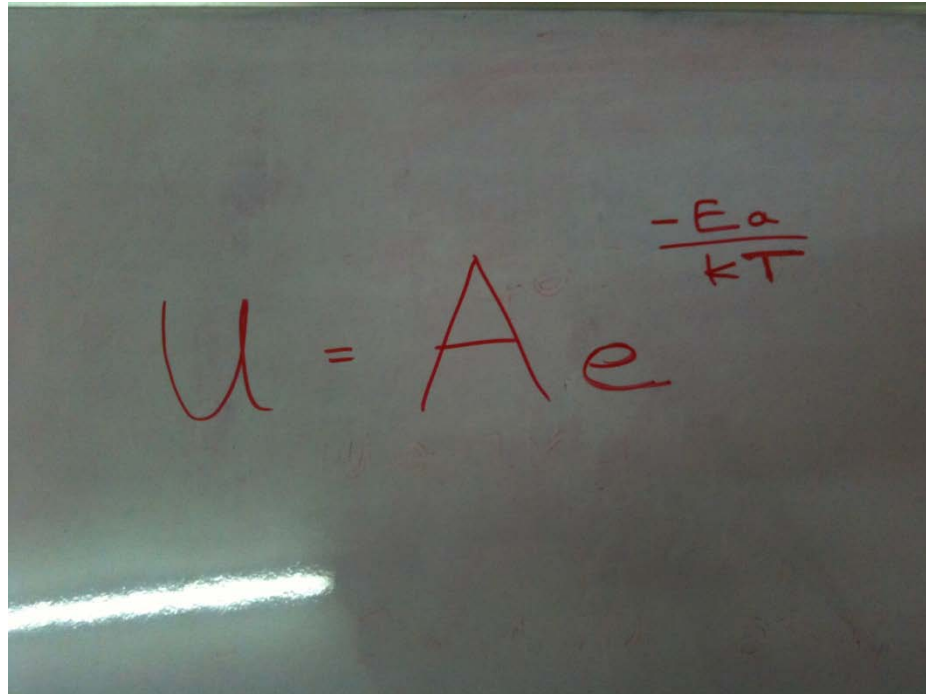
10 cm cubed of 37% Formaldehyde Solution +
1 L of Distilled Water + (after 24 hours)
1 g of Phenolphthalein.

Theory – Continued.

- Mix equal volumes of both solutions.
- After some time, 'delta T', the solution turns pink.

The Equations and the Math.

- The rate of the reaction is governed by the Arrhenius Equation.



A photograph of a chalkboard with the Arrhenius equation written in red chalk. The equation is $u = A e^{-\frac{E_a}{RT}}$. The 'u' is on the left, followed by an equals sign, then a large 'A', then 'e' with a superscripted fraction $-\frac{E_a}{RT}$.

The Equation and the Math.

- $u \rightarrow$ the reaction speed.
- $A \rightarrow$ a constant.
- $E_a \rightarrow$ energy of activation.
- $K \rightarrow$ the Boltzmann Constant.
- $T \rightarrow$ the temperature (in Kelvin) at which the reaction occurred.

The Equation and the Math – The Linear Form.

$$u = A e^{-\frac{E_a}{KT}}$$

$$\ln(u) = \ln A + \ln e^{-\frac{E_a}{KT}}$$

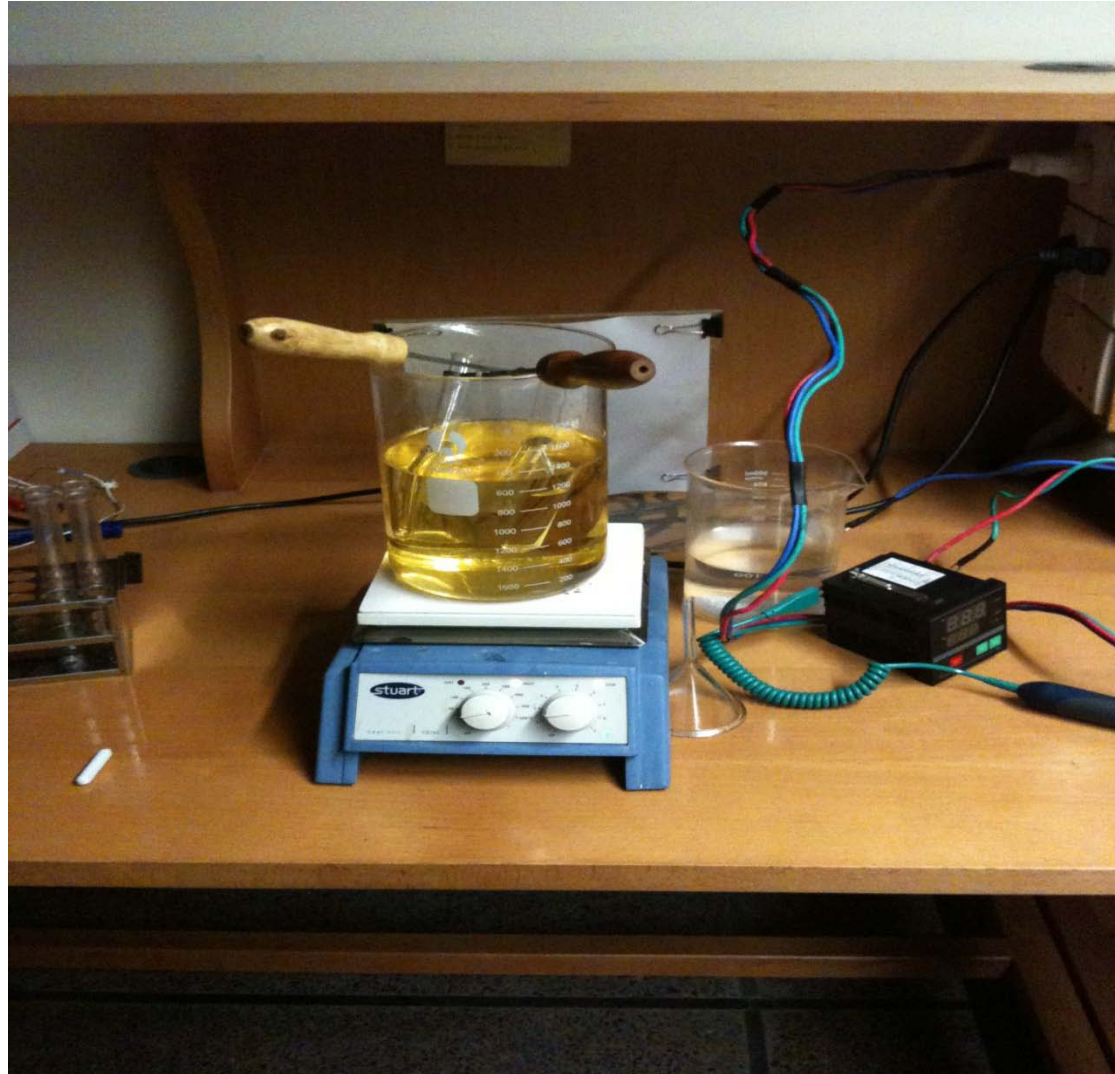
$$\ln(u) = -\frac{1}{K} \left(\frac{E_a}{T} \right) + \ln A$$

$$Y = mX + C$$

The Experimental Setup – Equipment

- A hot plate.
- Magnetic Stirrer to distribute heat uniformly.
- A Temperature Probe.
- Oil Bath.
- Test Tubes.
- Stop Watch.
- Funnel.

The Experimental Setup – A Snapshot.



The Experiment.

- 5 cm cubed of each solution was placed in separate test tubes. The test tubes were half immersed in the oil bath the temperature of which was monitored constantly.
- After 5 minutes the two solutions were mixed and the stopwatch was started simultaneously.

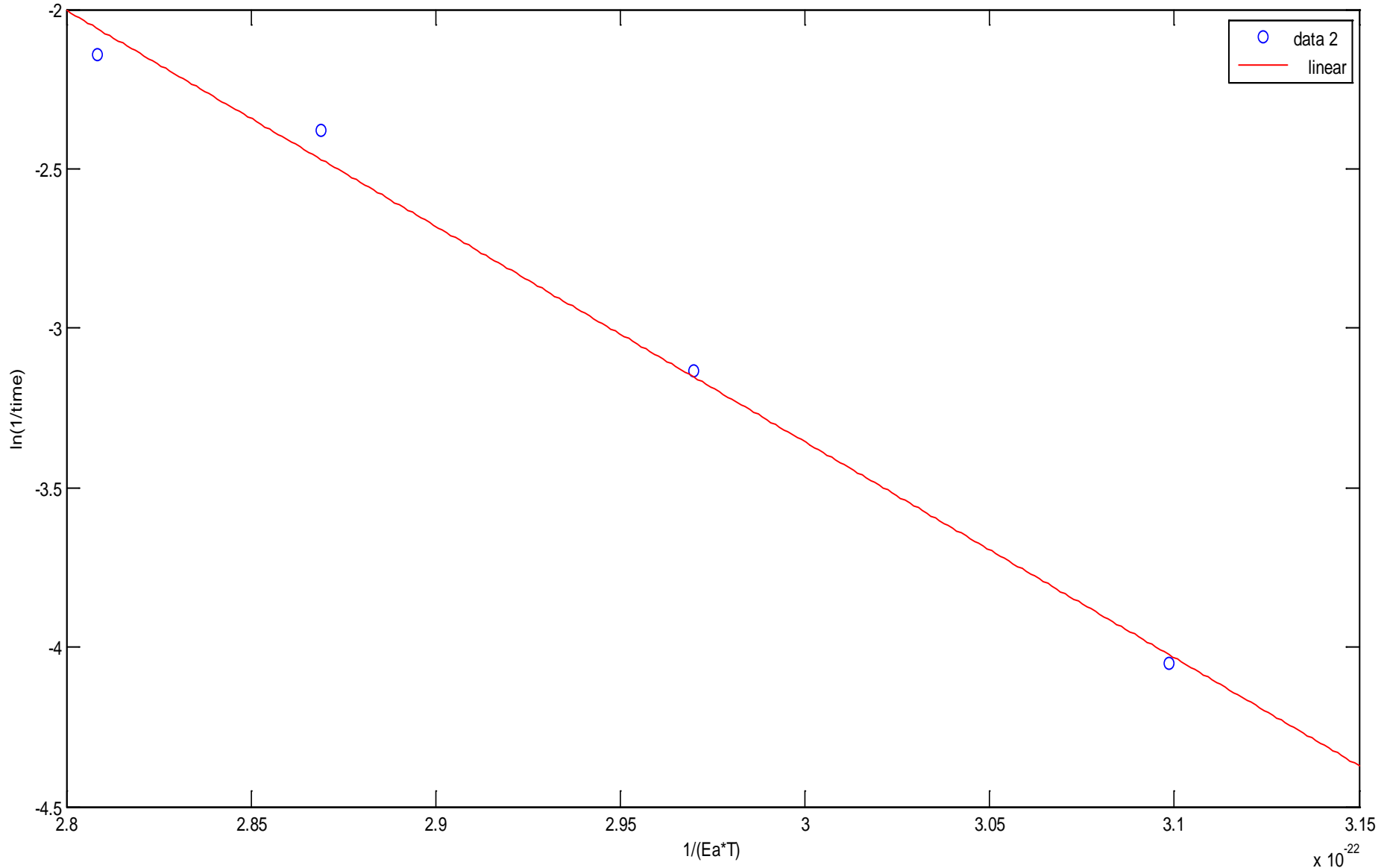
The Experiment – Continued.

- The stopwatch was stopped the instant the pink color appeared.
- The experiment was repeated three times at the same temperature.
- The entire procedure was repeated at 27, 40, 51 and 58 degrees Celsius.

Results

- The value of the Activation Energy was taken from literature.
- $E_a = 9.30 \times (10^{22}) \text{ J}$.
- A graph of $\ln(1/\text{time})$ against $E_a/\text{Temperature}$ was plotted.

Results – The Graph.



The Boltzmann Constant.

$$\text{Gradient} = -6.7659 \times (10)^{22}$$

$$(-1/k) = -6.7659 \times (10)^{22}$$

$$k = 1.478 \times (10)^{-23} \text{ J/K}$$

Error.

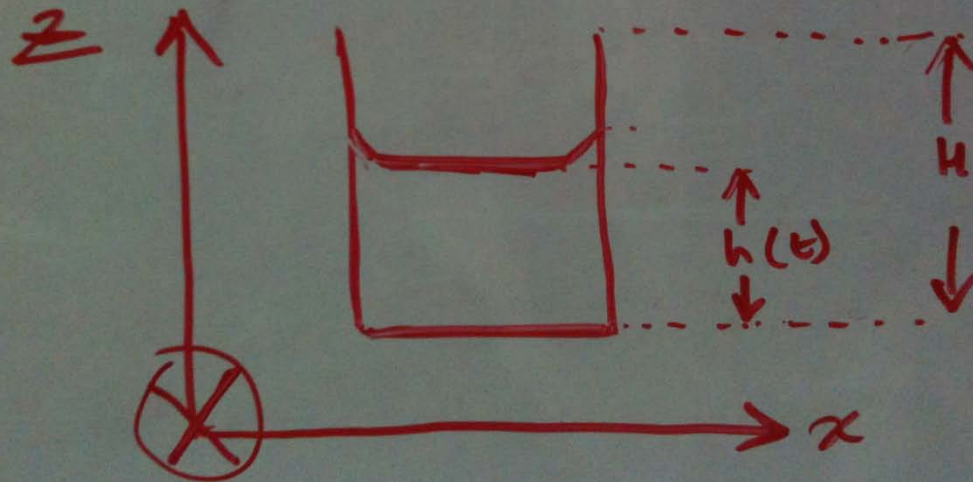
- The percentage error comes to about 9.8% when compared to the literature values.
- Reasonable estimation of the Boltzmann Constant.

The Evaporation of Ethanol – Theory.

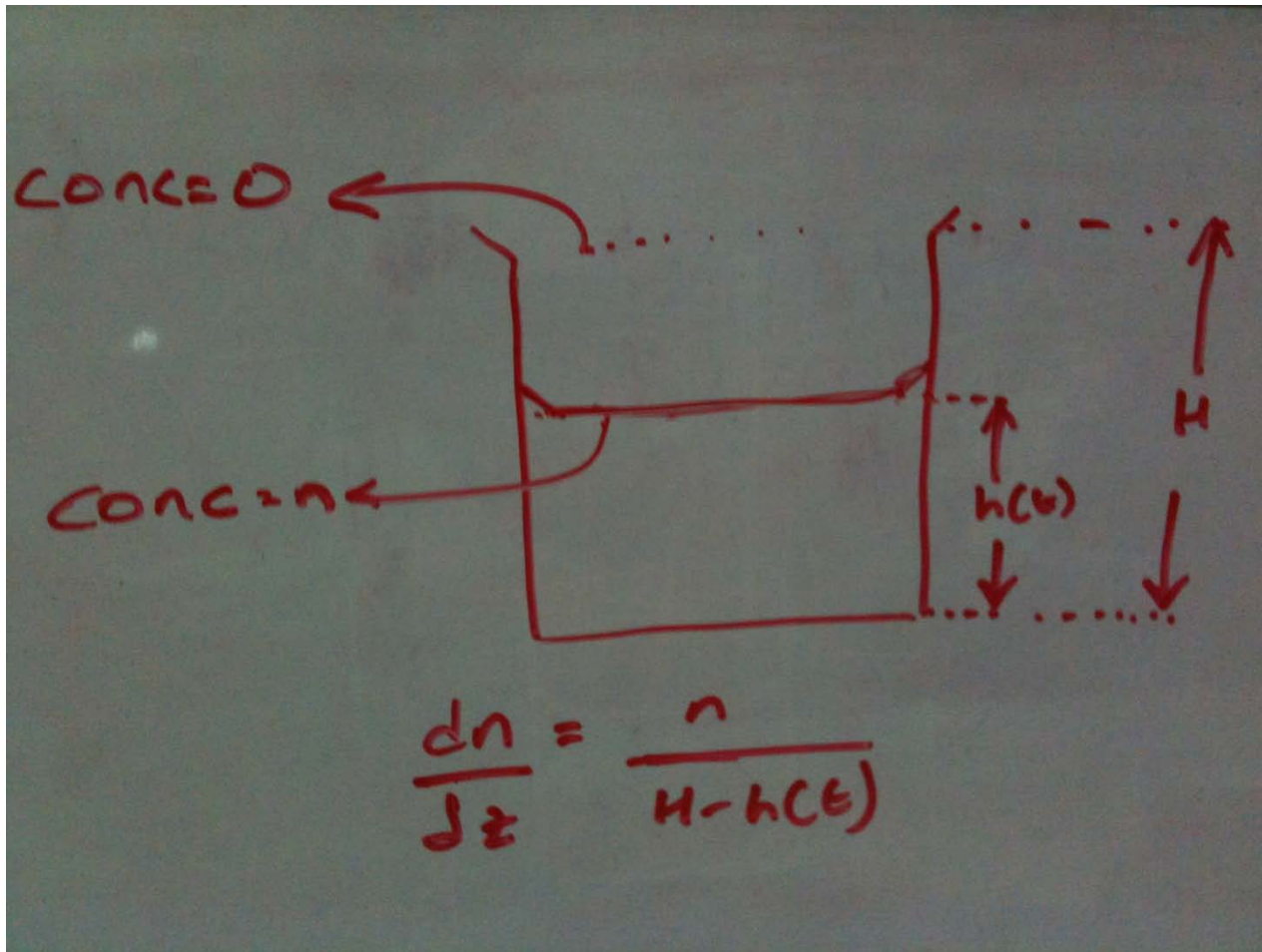
- The 4 Assumptions:
 1. The concentration of Ethanol outside the container is zero.
 2. There exists no temperature gradient within the bulk of the liquid.
 3. There exists a steady flow of air outside the container.
 4. Above the surface of the Ethanol there exist saturated vapors of Ethanol.

Theory – Fick's Diffusion Law.

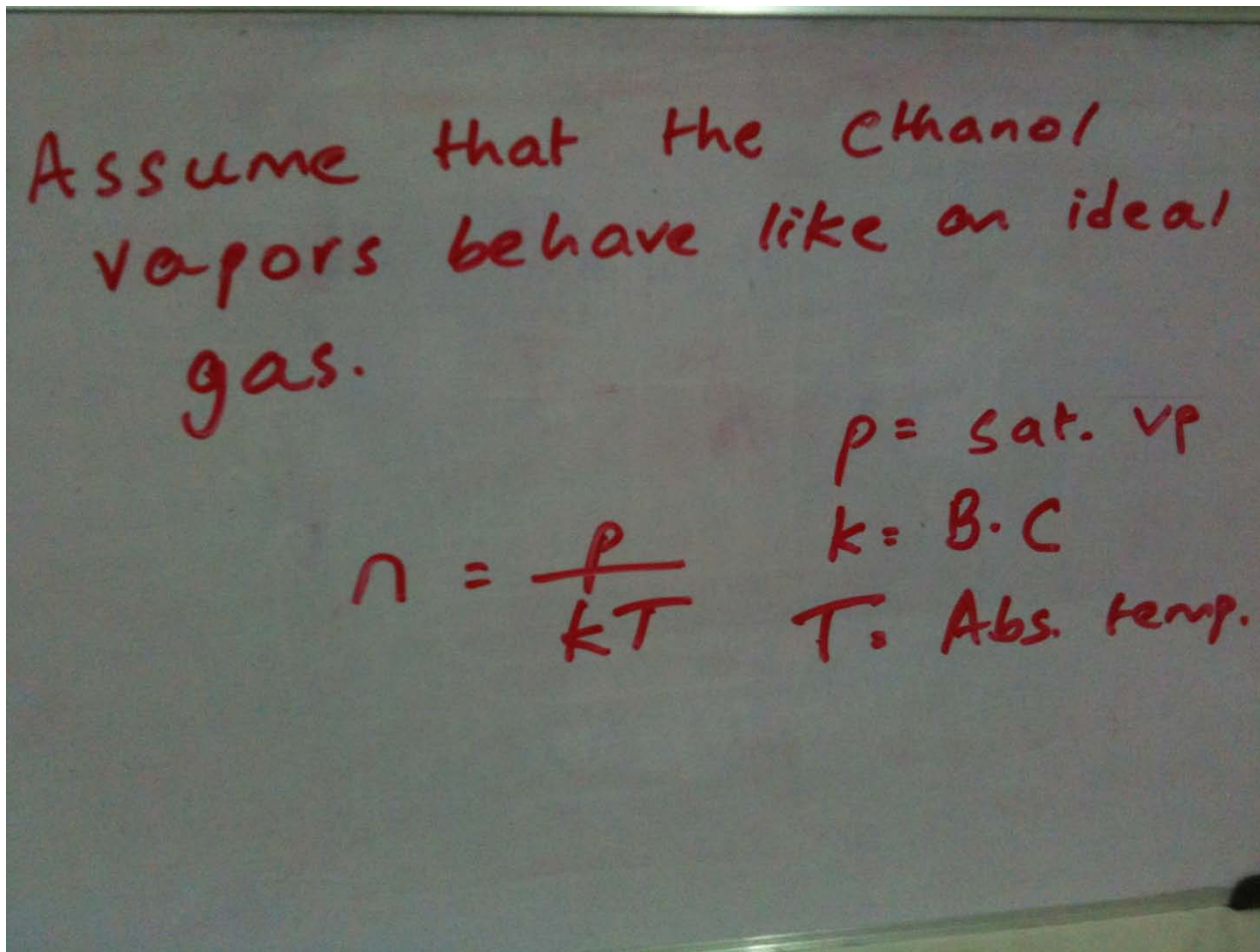
$$\frac{dN}{dt} = -DS \frac{dn}{dz}$$



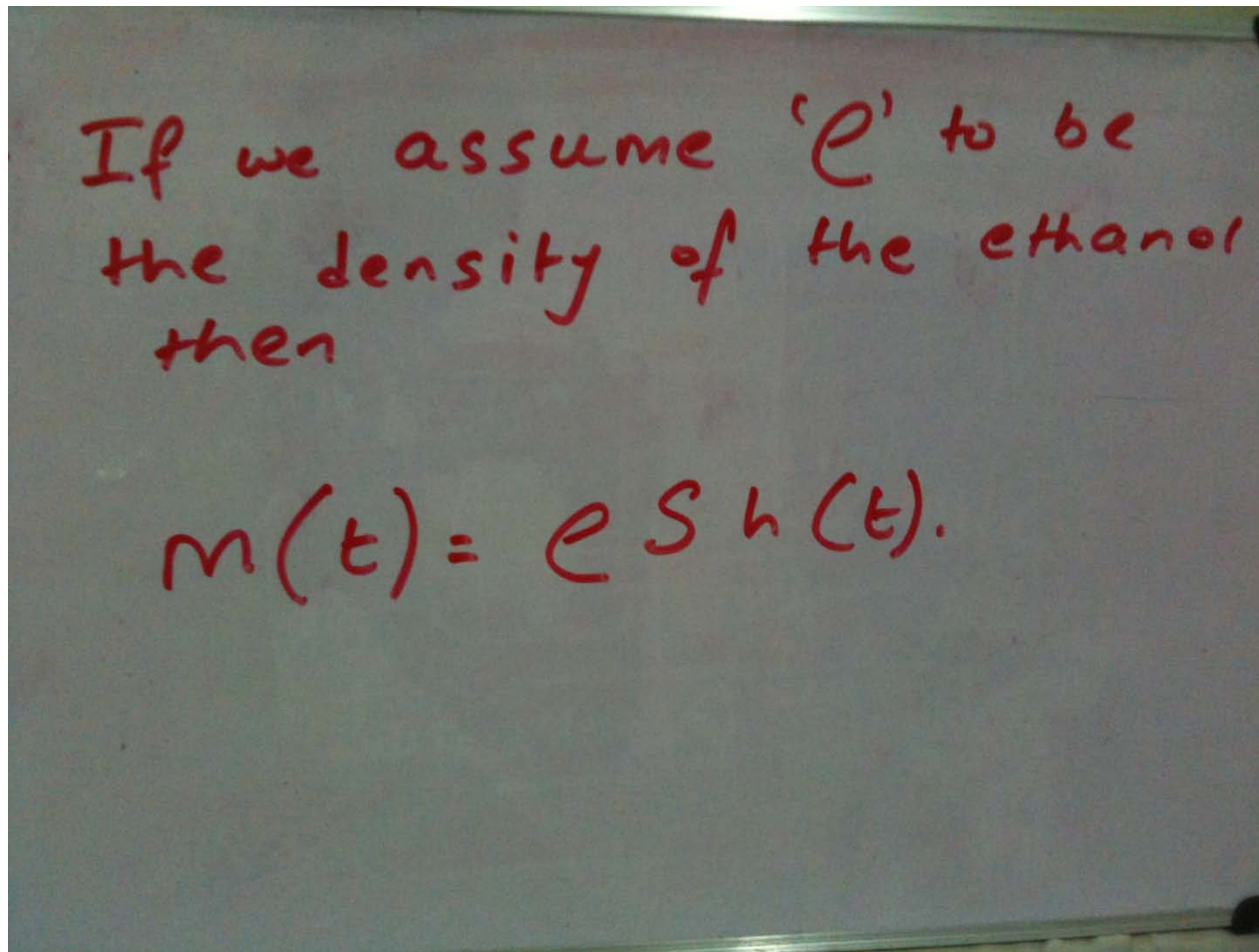
Theory – Assumption # 1



Theory – Another Assumption.



Theory – Yet Another Assumption.



Fick's Law after Assumption # 5, 6 & 7

$$\frac{dN}{dt} = -DS \frac{P}{KT} \frac{eS}{e_{HS-m(t)}}$$

After a Lot of Math.

By mathematical
manipulation.

$$\frac{dm(t)}{dt} = \frac{C_1 P \sqrt{T}}{C_2 - m(t)}$$

Yet Another Assumption.

$$\frac{dm}{dt} = c_3 \frac{1}{c_2 - m(t)}$$

$$c_3 = P\sqrt{T} c_1$$

After some more Math.

$$K = \frac{9 (c_3)^2 (\pi)^3 m_0 d^4 (p_0^2)}{4 s^4 e^2 (m_a)^2 p^2 T}$$

C3

$$C_3 = \frac{dm(t)}{dt} [m(t) - C_2]$$

The Experimental Setup – A Snapshot.



The Experiment – Software Used.

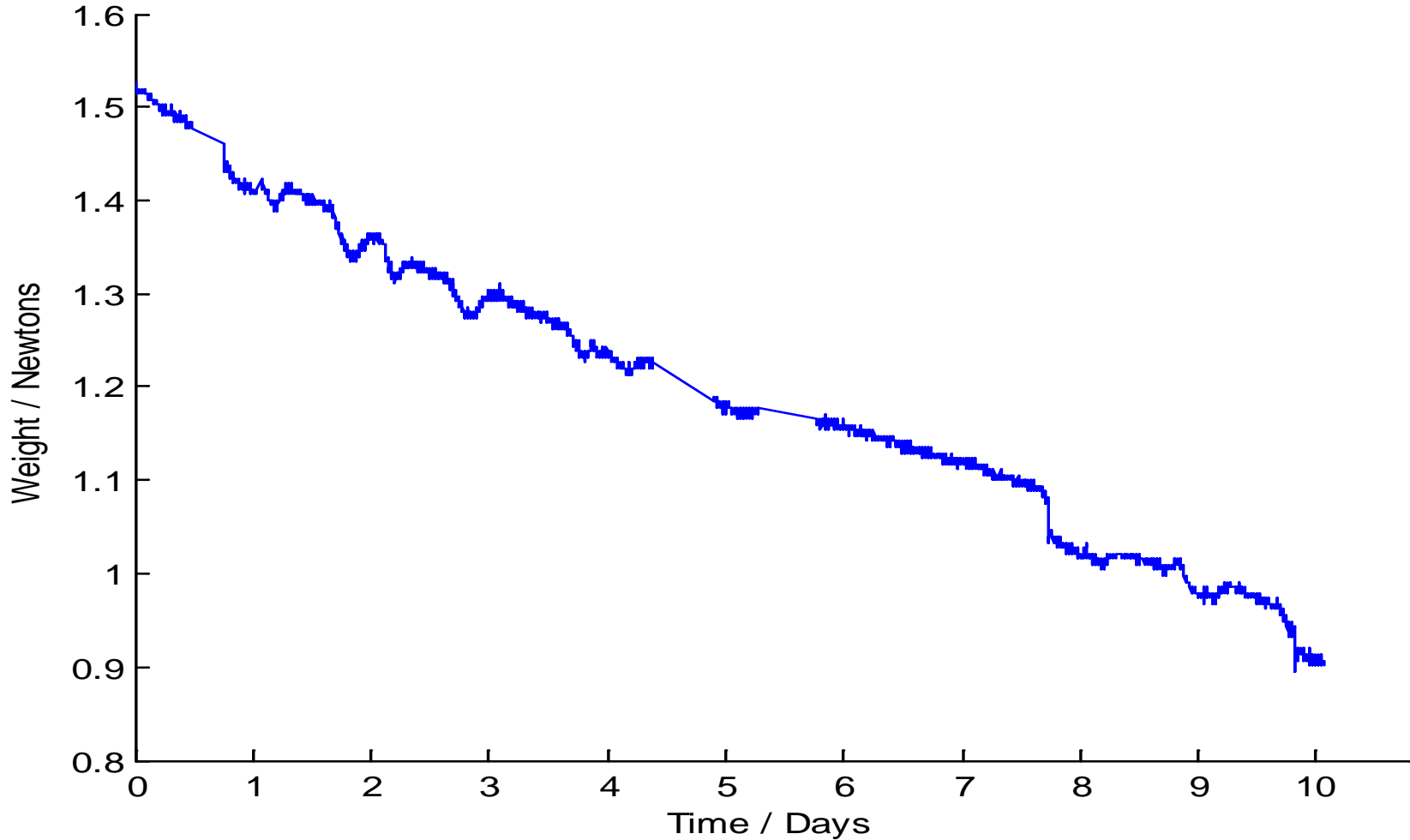
- Labview → To check the temperature variations. It was determined that they were not significant.
- Logger Pro → Interfaces Lab Pro with the computer. Lab Pro gathered information from the...
- Force Sensor (device) → Measured the weight of the alcohol after every 100 seconds.

The Disaster.

- On the 12th of June, the experiment was started. On the 6th day, three consecutive power failures caused the data collected to crash.
- A re-run was immediately started.
- The experiment which was scheduled to finish on the 22nd now finished on the 27th.

The Results on the 27th.

Weight vs. Time



Some Problems.

- On Monday morning, 5 grams of the Ethanol were unaccounted for.
- On Wednesday, 1 gram of Ethanol was unaccounted for.
- Restricted to two parts of the graph and not the entire graph as a whole.
- The evaporation procedure was not yet complete.

What to do now?

1. Evaluate the Boltzmann constant for the two separate parts.
2. Theoretically account for the mass loss.

Apologies.

- I have not yet been able to calculate the Boltzmann constant through the evaporation of ethanol. However considering the nice trend of the graph and the good behavior of temperature I can be confident of a highly accurate answer.

Thank you !